

▼ When to Optimize

▼ Enumerating all possible plans

- Selection Pushdown
- Join Conversion
- Join Reordering
- Pick a Join Algo

▼ Which Plan is the Best?

- Always push down selections
- Always convert joins
- Which join order???
- Which join algo?

▼ What makes a plan the best?

- Idea 2: IO Cost
- Idea 1: CPU Cost

▼ IO Cost

▼ Overview

▼ How do we measure IO Cost?

- Number of reads performed by each operator
- Number of writes performed by each operator

▼ What about communicating between operators?

- Assume operators can communicate with each other for free.

▼ Costs only include:

- The cost of materializing the data IF it needs to be materialized on disk
- The cost of reading the data back in IF it needs to be read back in.

▼ What else do we need?

- For some of these estimates, we'll need to be able to estimate the size of each table (call the # of pages in R: $|R|$)

▼ Basic properties of the data:

- Key Columns
- Distribution of Values

▼ IO Costs

▼ File Scan (R)

- Number of IOs : $|R|$

▼ Selection ($\sigma(R)$)

- Number of IOs : 0 (never need to materialize a selection)

▼ Index Lookup ($\sigma(R)$ where R is a file scan)

▼ Number of IOs for a Hash Index : $|\sigma(R)|$

- How big is this? Return to it later.

- Number of IOs for a B+Tree Index with directory pages of size B: $|\sigma(R)| + \log_B(|R|)$

▼ Projection ($\pi(R)$)

- Number of IOs : 0 (never need to materialize a projection)

▼ Union

- Number of IOs : 0 (never need to materialize a BAG union — see distinct for set union)

▼ Sort ($\tau(R)$) — External Sort with B pages of memory

- Number of IOs : $\sim 2 \cdot \log_B(|R| / 2)$
- ▼ **Cross-Product ($R \times S$) — BNLJ with B pages of memory for blocking R**
 - ▼ Number of IOs : $|S| + (|R| / B) \cdot (|S|)$
 - Need to write all of S to disk once: $|S|$ pages
 - ▼ Repeat $(|R| / B)$ times...
 - Read B pages of data from source operator R: Free
 - Join the block with the materialized data in S, one tuple at a time: $|S|$
- ▼ **Join ($R \bowtie S$) — 1-pass Hash/Tree Join**
 - Number of IOs: 0 (entirely in-memory)
- ▼ **Join ($R \bowtie S$) — 2-pass Hash Join**
 - ▼ Number of IOs: $2 \cdot (|R| + |S|)$
 - Write all $|R|$ and $|S|$ to disk, bucketizing: $|R| + |S|$
 - Read in each bucket: $|R| + |S|$
- ▼ **Join ($\tau(R) \bowtie \tau(S)$) — Sort/Merge Join**
 - Number of IOs: 0 + cost of the $\tau(S)$ (Merge step is free)
- ▼ **Join ($R \bowtie_{R.A = S.A} S$) — Index Nested Loop Join (assuming index on S)**
 - ▼ Number of IOs: $|R| \cdot [\text{cost of one index lookup: } \sigma_{[const] = S.A}(S)]$
 - Each inner loop is basically one Index Scan
- ▼ **Aggregation ($\gamma(R)$) — In-memory**
 - Number of IOs: 0
- ▼ **Aggregation ($\gamma(R)$) — On-Disk, Hash-Based**
 - ▼ Number of IOs: $2|R|$
 - Write each bucket out, read each bucket in
- ▼ **Aggregation ($\gamma(\tau(R))$) — On-Disk, Sort-Based**
 - Number of IOs: 0 + cost of $\tau(R)$
- **Distinct ($\delta(R)$) — Works EXACTLY like Aggregation**

▼ Cardinality (Size) Estimation

- ▼ Most of the operators are straightforward
 - $\pi(R), \tau(R) : |R|$
 - $R \cup S : |R| + |S|$
 - $R \times S : |R| * |S|$
 - $R \bowtie S : \text{Identical to } \sigma(R \times S) \dots$
- ▼ Some are hard
 - $\sigma(R)$
 - $\gamma(R)$ & $\delta(R)$
- ▼ Selection : Compute Selectivity (or % tuples passed through)
 - ▼ **Generic (Default) Heuristic:**
 - Selectivity = 0.5
 - Works ... mostly well 70% of the time. Very brittle and liable to break things
 - **Be wary:** DBMSes actually do this!
 - ▼ **R.A = [Const]**
 - If R.A is a Key, then precisely 1 tuple passes through... given
 - ▼ **Idea:** Collect stats: # of distinct values
 - Selectivity = $1 / \#$ of distinct values of R.A

- Works well... but only for discrete data (Strings, Ints, Dates)
- Also gives you “Key” for free
- Also works for R.A in [List]
- ▼ R.A < [Const] (also works for others)
 - ▼ **Idea:** Collect stats: Min/Max, and assume a uniform distribution of values
 - Selectivity = $([Const] - Min) / (Max - Min)$
 - Works for continuous data (Floats)
 - ▼ R.A = R.B
 - (the Equijoin condition)
 - ▼ **Idea 1:** Assume no correlation
 - Becomes identical to either R.A = const or R.B = const
 - For each row, you’re testing whether R.B = Some specific, somewhat arbitrary value
 - **Both** are an upper bound on the selectivity, so take whichever reduction gives you the lower value
 - ▼ C1 AND C2
 - Assuming no correlation between C1 and C2: $Selectivity(C1) \cdot Selectivity(C2)$
- Going more fancy: Histograms (See attached)